

## High School Conceptual Progressions Model Course 1 - Bundle 1 Interactions Between Objects (Macroscopic)



*This is the first bundle of the High School Conceptual Progressions Model Course 1. Each bundle has connections to the other bundles in the course, as shown in the [Course Flowchart](#).*

*Bundle 1 Question: This bundle is assembled to address the question “How do objects such as moons and satellites orbit the sun and/or planets such as the Earth?”*

### **Summary**

The bundle organizes performance expectations with a focus on helping students understand *how objects move and interact*. Instruction developed from this bundle should always maintain the three-dimensional nature of the standards, but recognize that instruction is not limited to the practices and concepts directly linked with any of the bundle performance expectations.

### **Connections between bundle DCIs**

The Big Bang theory is supported by observations of distant galaxies receding from our own, of the measured composition of stars and non-stellar gases, and of the maps of spectra of the primordial radiation that still fills the universe (ESS1.A as in HS-ESS1-2). The measured composition of stars and the movements of different galaxies connect the ideas of an atom’s emission and absorption of characteristic frequencies of light (PS4.B as in HS-ESS1-2) with the idea that the study of stars’ light spectra and brightness is used to identify compositional elements of stars, their movements, and their distances from Earth (ESS1.A as in HS-ESS1-2, HS-ESS1-3).

Concepts related to the movement of different galaxies (PS4.B as in HS-ESS1-2) connect to the ideas of forces at a distance are explained by fields (PS2.B as in HS-PS2-4). These ideas of force then connect to concepts of Kepler’s laws, which describe common features of the motions of orbiting objects, including their elliptical paths around the sun (ESS1.B as in HS-ESS1-4). Also, these ideas connect to the concept that Newton’s second law accurately predicts changes in the motion of macroscopic objects (PS1.A as in HS-PS2-1).

### **Bundle Science and Engineering Practices**

Instruction leading to this bundle of PEs will help students build toward proficiency in elements of the practices of using models (HS-PS2-1); using mathematical representations (HS-PS2-4 and HS-ESS1-4); and constructing an explanation (HS-ESS1-2). Many other practice elements can be used in instruction.

### **Bundle Crosscutting Concepts**

Instruction leading to this bundle of PEs will help students build toward proficiency in elements of the crosscutting concepts of Patterns (HS-PS2-4), Cause and Effect (HS-PS2-1), Scale, Proportion, and Quantity (HS-ESS1-4), and Energy and Matter (HS-ESS1-2). Many other CCC elements can be used in instruction.

*All instruction should be three-dimensional.*

<p><b>Performance Expectations</b></p> <p>HS-PS2-4 is partially assessable</p>	<p>HS-PS2-1. <b>Analyze data to support the claim that Newton’s second law of motion describes the mathematical relationship among the net force on a macroscopic object, its mass, and its acceleration.</b> [Clarification Statement: Examples of data could include tables or graphs of position or velocity as a function of time for objects subject to a net unbalanced force, such as a falling object, an object rolling down a ramp, or a moving object being pulled by a constant force.] [Assessment Boundary: Assessment is limited to one-dimensional motion and to macroscopic objects moving at non-relativistic speeds.]</p> <p>HS-PS2-4. <b>Use mathematical representations of Newton’s Law of Gravitation and Coulomb’s Law to describe and predict the gravitational and electrostatic forces between objects.</b> [Clarification Statement: Emphasis is on both quantitative and conceptual descriptions of gravitational and electric fields.] [Assessment Boundary: Assessment is limited to systems with two objects.]</p> <p>HS-ESS1-2. <b>Construct an explanation of the Big Bang theory based on astronomical evidence of light spectra, motion of distant galaxies, and composition of matter in the universe.</b> [Clarification Statement: Emphasis is on the astronomical evidence of the red shift of light from galaxies as an indication that the universe is currently expanding, the cosmic microwave background as the remnant radiation from the Big Bang, and the observed composition of ordinary matter of the universe, primarily found in stars and interstellar gases (from the spectra of electromagnetic radiation from stars), which matches that predicted by the Big Bang theory (3/4 hydrogen and 1/4 helium).]</p> <p>HS-ESS1-4. <b>Use mathematical or computational representations to predict the motion of orbiting objects in the solar system.</b> [Clarification Statement: Emphasis is on Newtonian gravitational laws governing orbital motions, which apply to human-made satellites as well as planets and moons.] [Assessment Boundary: Mathematical representations for the gravitational attraction of bodies and Kepler’s Laws of orbital motions should not deal with more than two bodies, nor involve calculus.]</p>
<p><b>Example Phenomena</b></p>	<p>The moon is not observed in the same place in the sky at the same time or in the same way every night.</p> <p>Satellites in orbit do not regularly come crashing down to the surface of the Earth.</p>
<p><b>Additional Practices Building to the PEs</b></p>	<p><b>Asking Questions and Defining Problems</b></p> <ul style="list-style-type: none"> <li>Ask questions that arise from examining models or a theory, to clarify and/or seek additional information and relationships. Students could <i>ask questions to clarify the</i> [cause and effect relationship between] <b><i>the motions of orbiting objects and the gravitational effects from, or collisions with, other objects in the solar system.</i></b> HS-PS2-4 and HS-ESS1-4</li> </ul> <p><b>Developing and Using Models</b></p> <ul style="list-style-type: none"> <li>Develop and/or use multiple types of models to provide mechanistic accounts and/or predict phenomena, and move flexibly between model types based on merits and limitations. Students could <i>use a [computer] model or develop a drawn model</i> to <b><i>describe common features of the motions of orbiting objecting, including their elliptical paths around the sun or show how orbits may change due to the gravitational effects from, or collisions with, other objects in the solar system.</i></b> HS-ESS1-4</li> </ul> <p><b>Planning and Carrying Out Investigations</b></p> <ul style="list-style-type: none"> <li>Make directional hypotheses that specify what happens to a dependent variable when an independent variable is manipulated. Students could <i>plan and carry out an investigation [including] making a directional hypothesis</i> <b><i>predicting changes in the motion of macroscopic objects.</i></b> HS-PS2-1</li> </ul> <p><b>Analyzing and Interpreting Data</b></p> <ul style="list-style-type: none"> <li>Evaluate the impact of new data on a working explanation and/or model of a proposed process or system. Students could <i>evaluate the impact of new data on a working explanation and/or model</i> [used] to <b><i>predict the motion of orbiting objects in the solar system due to the effects of gravitational forces.</i></b> HS-PS2-4 and HS-ESS1-4</li> </ul>

<p><b>Additional Practices Building to the PEs (Continued)</b></p>	<p><b>Using Mathematical and Computational Thinking</b></p> <ul style="list-style-type: none"> <li>Apply techniques of algebra and functions to represent and solve scientific and engineering problems. Students could <i>apply techniques of algebra and functions to represent and solve scientific problems</i> [related to] <b><i>the Big Bang theory</i></b> [which is supported by] <b><i>astronomical evidence of light spectra, motion of distant galaxies, and composition of matter in the universe.</i></b> HS-ESS1-2</li> </ul> <p><b>Constructing Explanations and Designing Solutions</b></p> <ul style="list-style-type: none"> <li>Design, evaluate, and/or refine a solution to a complex real-world problem, based on scientific knowledge, student-generated sources of evidence, prioritized criteria, and tradeoff considerations. Students could <i>evaluate and/or refine a solution to a complex real-world problem</i> [by] <b><i>describing common features of the motions of orbiting objects, including their elliptical paths around the sun and how their orbits may change due to the gravitational effects from, or collisions with, other objects in the solar system.</i></b> HS-PS2-1, HS-PS2-4, and HS-ESS1-4</li> </ul> <p><b>Engaging in Argument from Evidence</b></p> <ul style="list-style-type: none"> <li>Evaluate the claims, evidence, and/or reasoning behind currently accepted explanations or solutions to determine the merits of arguments. Students could <i>evaluate the claims, evidence, and/or reasoning</i> [for how] <b><i>the Big Bang Theory is supported by observations of distant galaxies receding from our own, of the measured composition of stars and non-stellar gases, and of the maps of spectra of the primordial radiation that still fills the universe.</i></b> HS-ESS1-2</li> </ul> <p><b>Obtaining, Evaluating, and Communicating Information</b></p> <ul style="list-style-type: none"> <li>Communicate scientific and/or technical information or ideas (e.g. about phenomena and/or the process of development and the design and performance of a proposed process or system) in multiple formats (including orally, graphically, textually, and mathematically). Students could <i>communicate scientific and/or technical information in multiple formats</i> [for how] <b><i>stars' light spectra and brightness is used to identify compositional elements of stars, their movements, and their distances from Earths.</i></b> HS-ESS1-2</li> </ul>
<p><b>Additional Crosscutting Concepts Building to the PEs</b></p>	<p><b>Patterns</b></p> <ul style="list-style-type: none"> <li>Classifications or explanations used at one scale may fail or need revision when information from smaller or larger scales is introduced; thus requiring improved investigations and experiments. Students could analyze <b><i>changes in the motion of macroscopic objects such as the motion of orbiting objects in the solar system</i></b> [to determine if an] <i>explanation at one scale may fail or need revision when</i> [compared to a different] <i>scale.</i> HS-PS2-1 and HS-ESS1-4</li> </ul>

<p><b>Additional Crosscutting Concepts Building to the PEs (Continued)</b></p>	<p><b>Cause and Effect</b></p> <ul style="list-style-type: none"> <li>• Cause and effect relationships can be suggested and predicted for complex natural and human designed systems by examining what is known about smaller scale mechanisms within the system. Students could analyze and interpret data about the <i>cause and effect relationships</i> [between objects] <i>at a smaller scale to predict the motion of orbiting objects, including their elliptical paths around the sun or how orbits may change due to the gravitational effects from, or collisions with, other objects in the solar system.</i> HS-ESS1-4</li> </ul> <p><b>Systems and System Models</b></p> <ul style="list-style-type: none"> <li>• Models (e.g., physical, mathematical, computer models) can be used to simulate systems and interactions—including energy, matter, and information flows—within and between systems at different scales. Students could describe how <i>models can be used to simulate systems and interactions within and between systems at different scales</i> [for how] <i>Newton’s law of gravitation provides the mathematical model to describe and predict the effects of gravitational forces between distant objects.</i> HS-PS2-4</li> </ul>
<p><b>Additional Connections to Nature of Science</b></p>	<p><b>Scientific Investigations Use a Variety of Methods (SEP):</b></p> <ul style="list-style-type: none"> <li>• Scientific investigations use a variety of methods, tools, and techniques to revise and produce new knowledge. Students could <i>obtain, evaluate, and communicate information about how scientific methods, tools, and techniques used to gather observations [empirical evidence] to support the Big Bang Theory</i> [have changed over time, enabling scientists to come to their current understandings]. HS-ESS1-2</li> </ul> <p><b>Science is a Way of Knowing (CCC):</b></p> <ul style="list-style-type: none"> <li>• Science knowledge has a history that includes the refinement of, and changes to, theories, ideas, and beliefs over time. Students could ask questions about how <i>science knowledge has changed over time</i> [about how] <i>Kepler’s laws describe common features of the motions of orbiting objects, including their elliptical paths around the sun.</i> HS-ESS1-4</li> </ul>

## HS-PS2-1

Students who demonstrate understanding can:

**HS-PS2-1. Analyze data to support the claim that Newton’s second law of motion describes the mathematical relationship among the net force on a macroscopic object, its mass, and its acceleration.** [Clarification Statement: Examples of data could include tables or graphs of position or velocity as a function of time for objects subject to a net unbalanced force, such as a falling object, an object rolling down a ramp, or a moving object being pulled by a constant force.] [Assessment Boundary: Assessment is limited to one-dimensional motion and to macroscopic objects moving at non-relativistic speeds.]

The performance expectation above was developed using the following elements from *A Framework for K-12 Science Education*:

Science and Engineering Practices	Disciplinary Core Ideas	Crosscutting Concepts
<p><b>Analyzing and Interpreting Data</b> Analyzing data in 9–12 builds on K–8 and progresses to introducing more detailed statistical analysis, the comparison of data sets for consistency, and the use of models to generate and analyze data.</p> <ul style="list-style-type: none"> <li>Analyze data using tools, technologies, and/or models (e.g., computational, mathematical) in order to make valid and reliable scientific claims or determine an optimal design solution.</li> </ul> <p>-----</p> <p style="text-align: center;"><b>Connections to Nature of Science</b></p> <p><b>Science Models, Laws, Mechanisms, and Theories Explain Natural Phenomena</b></p> <ul style="list-style-type: none"> <li>Theories and laws provide explanations in science.</li> <li>Laws are statements or descriptions of the relationships among observable phenomena.</li> </ul>	<p><b>PS2.A: Forces and Motion</b></p> <ul style="list-style-type: none"> <li>Newton’s second law accurately predicts changes in the motion of macroscopic objects.</li> </ul>	<p><b>Cause and Effect</b></p> <ul style="list-style-type: none"> <li>Empirical evidence is required to differentiate between cause and correlation and make claims about specific causes and effects.</li> </ul>

### Observable features of the student performance by the end of the course:

1	Organizing data	
	a	Students organize data that represent the net force on a macroscopic object, its mass (which is held constant), and its acceleration (e.g., via tables, graphs, charts, vector drawings).
2	Identifying relationships	
	a	Students use tools, technologies, and/or models to analyze the data and identify relationships within the datasets, including:
		i. A more massive object experiencing the same net force as a less massive object has a smaller acceleration, and a larger net force on a given object produces a correspondingly larger acceleration; and
		ii. The result of gravitation is a constant acceleration on macroscopic objects as evidenced by the fact that the ratio of net force to mass remains constant.
3	Interpreting data	
	a	Students use the analyzed data as evidence to describe* that the relationship between the observed quantities is accurately modeled across the range of data by the formula $a = F_{net}/m$ (e.g., double force yields double acceleration, etc.).
	b	Students use the data as empirical evidence to distinguish between causal and correlational relationships linking force, mass, and acceleration.
	c	Students express the relationship $F_{net}=ma$ in terms of causality, namely that a net force on an object causes the object to accelerate.

## HS-PS2-4

Students who demonstrate understanding can:

**HS-PS2-4. Use mathematical representations of Newton’s Law of Gravitation and Coulomb’s Law to describe and predict the gravitational and electrostatic forces between objects.** [Clarification Statement: Emphasis is on both quantitative and conceptual descriptions of gravitational and electric fields.] [Assessment Boundary: Assessment is limited to systems with two objects.]

The performance expectation above was developed using the following elements from *A Framework for K-12 Science Education*:

Science and Engineering Practices	Disciplinary Core Ideas	Crosscutting Concepts
<p><b>Using Mathematics and Computational Thinking</b> Mathematical and computational thinking at the 9–12 level builds on K–8 and progresses to using algebraic thinking and analysis; a range of linear and nonlinear functions including trigonometric functions, exponentials and logarithms; and computational tools for statistical analysis to analyze, represent, and model data. Simple computational simulations are created and used based on mathematical models of basic assumptions.</p> <ul style="list-style-type: none"> <li>Use mathematical representations of phenomena to describe explanations.</li> </ul> <hr style="border-top: 1px dashed #ccc;"/> <p style="text-align: center;"><b>Connections to Nature of Science</b></p> <p><b>Science Models, Laws, Mechanisms, and Theories Explain Natural Phenomena</b></p> <ul style="list-style-type: none"> <li>Theories and laws provide explanations in science.</li> <li>Laws are statements or descriptions of the relationships among observable phenomena.</li> </ul>	<p><b>PS2.B: Types of Interactions</b></p> <ul style="list-style-type: none"> <li>Newton’s law of universal gravitation and Coulomb’s law provide the mathematical models to describe and predict the effects of gravitational and electrostatic forces between distant objects.</li> <li>Forces at a distance are explained by fields (gravitational, electric, and magnetic) permeating space that can transfer energy through space. Magnets or electric currents cause magnetic fields; electric charges or changing magnetic fields cause electric fields.</li> </ul>	<p><b>Patterns</b></p> <ul style="list-style-type: none"> <li>Different patterns may be observed at each of the scales at which a system is studied and can provide evidence for causality in explanations of phenomena.</li> </ul>

### Observable features of the student performance by the end of the course:

1	Representation	
	a	Students clearly define the system of the interacting objects that is mathematically represented.
	b	Using the given mathematical representations, students identify and describe* the gravitational attraction between two objects as the product of their masses divided by the separation distance squared ( $F_g = -G \frac{m_1 m_2}{d^2}$ ), where a negative force is understood to be attractive.
	c	Using the given mathematical representations, students identify and describe* the electrostatic force between two objects as the product of their individual charges divided by the separation distance squared ( $F_e = k \frac{q_1 q_2}{d^2}$ ), where a negative force is understood to be attractive.
2	Mathematical modeling	
	a	Students correctly use the given mathematical formulas to predict the gravitational force between objects or predict the electrostatic force between charged objects.
3	Analysis	
	a	Based on the given mathematical models, students describe* that the ratio between gravitational and electric forces between objects with a given charge and mass is a pattern that is independent of distance.

b	Students describe* that the mathematical representation of the gravitational field ( $F_g = -G \frac{m_1 m_2}{d^2}$ ) only predicts an attractive force because mass is always positive.
c	Students describe* that the mathematical representation of the electric field ( $F_e = k \frac{q_1 q_2}{d^2}$ ) predicts both attraction and repulsion because electric charge can be either positive or negative.
d	Students use the given formulas for the forces as evidence to describe* that the change in the energy of objects interacting through electric or gravitational forces depends on the distance between the objects.

## HS-ESS1-2

Students who demonstrate understanding can:

**HS-ESS1-2. Construct an explanation of the Big Bang theory based on astronomical evidence of light spectra, motion of distant galaxies, and composition of matter in the universe.** [Clarification Statement: Emphasis is on the astronomical evidence of the red shift of light from galaxies as an indication that the universe is currently expanding, the cosmic microwave background as the remnant radiation from the Big Bang, and the observed composition of ordinary matter of the universe, primarily found in stars and interstellar gases (from the spectra of electromagnetic radiation from stars), which matches that predicted by the Big Bang theory (3/4 hydrogen and 1/4 helium).]

The performance expectation above was developed using the following elements from *A Framework for K-12 Science Education*:

Science and Engineering Practices	Disciplinary Core Ideas	Crosscutting Concepts
<p><b>Constructing Explanations and Designing Solutions</b></p> <p>Constructing explanations and designing solutions in 9–12 builds on K–8 experiences and progresses to explanations and designs that are supported by multiple and independent student-generated sources of evidence consistent with scientific ideas, principles, and theories.</p> <ul style="list-style-type: none"> <li>Construct an explanation based on valid and reliable evidence obtained from a variety of sources (including students' own investigations, theories, simulations, peer review) and the assumption that theories and laws that describe the natural world operate today as they did in the past and will continue to do so in the future.</li> </ul> <p>-----</p> <p><b>Connections to Nature of Science</b></p> <p><b>Science Models, Laws, Mechanisms, and Theories Explain Natural Phenomena</b></p> <ul style="list-style-type: none"> <li>A scientific theory is a substantiated explanation of some aspect of the natural world, based on a body of facts that have been repeatedly confirmed through observation and experiment and the science community validates each theory before it is accepted. If new evidence is discovered that the theory does not accommodate, the theory is generally modified in light of this new evidence.</li> </ul>	<p><b>ESS1.A: The Universe and Its Stars</b></p> <ul style="list-style-type: none"> <li>The study of stars' light spectra and brightness is used to identify compositional elements of stars, their movements, and their distances from Earth.</li> <li>The Big Bang theory is supported by observations of distant galaxies receding from our own, of the measured composition of stars and non-stellar gases, and of the maps of spectra of the primordial radiation (cosmic microwave background) that still fills the universe.</li> <li>Other than the hydrogen and helium formed at the time of the Big Bang, nuclear fusion within stars produces all atomic nuclei lighter than and including iron, and the process releases electromagnetic energy. Heavier elements are produced when certain massive stars achieve a supernova stage and explode.</li> </ul> <p><b>PS4.B: Electromagnetic Radiation</b></p> <ul style="list-style-type: none"> <li>Atoms of each element emit and absorb characteristic frequencies of light. These characteristics allow identification of the presence of an element, even in microscopic quantities. (<i>secondary</i>)</li> </ul>	<p><b>Energy and Matter</b></p> <ul style="list-style-type: none"> <li>Energy cannot be created or destroyed—only moved between one place and another place, between objects and/or fields, or between systems.</li> </ul> <p>-----</p> <p><b>Connections to Engineering, Technology, and Applications of Science</b></p> <p><b>Interdependence of Science, Engineering, and Technology</b></p> <ul style="list-style-type: none"> <li>Science and engineering complement each other in the cycle known as research and development (R&amp;D). Many R&amp;D projects may involve scientists, engineers, and others with wide ranges of expertise.</li> </ul> <p>-----</p> <p><b>Connections to Nature of Science</b></p> <p><b>Scientific Knowledge Assumes an Order and Consistency in Natural Systems</b></p> <ul style="list-style-type: none"> <li>Scientific knowledge is based on the assumption that natural laws operate today as they did in the past and they will continue to do so in the future.</li> <li>Science assumes the universe is a vast single system in which basic laws are consistent.</li> </ul>

Observable features of the student performance by the end of the course:	
1	Articulating the explanation of phenomena
a	Students construct an explanation that includes a description* of how astronomical evidence from numerous sources is used collectively to support the Big Bang theory, which states that the universe is expanding and that thus it was hotter and denser in the past, and that the entire visible universe emerged from a very tiny region and expanded.
2	Evidence
a	Students identify and describe* the evidence to construct the explanation, including: <ul style="list-style-type: none"> <li>i. The composition (hydrogen, helium and heavier elements) of stars;</li> <li>ii. The hydrogen-helium ratio of stars and interstellar gases;</li> <li>iii. The redshift of the majority of galaxies and the redshift vs. distance relationship; and</li> <li>iv. The existence of cosmic background radiation.</li> </ul>
b	Students use a variety of valid and reliable sources for the evidence, which may include students' own investigations, theories, simulations, and peer review.
c	Students describe* the source of the evidence and the technology used to obtain that evidence.
3	Reasoning
a	Students use reasoning to connect evidence, along with the assumption that theories and laws that describe the natural world operate today as they did in the past and will continue to do so in the future, to construct the explanation for the early universe (the Big Bang theory). Students describe* the following chain of reasoning for their explanation: <ul style="list-style-type: none"> <li>i. Redshifts indicate that an object is moving away from the observer, thus the observed redshift for most galaxies and the redshift vs. distance relationship is evidence that the universe is expanding.</li> <li>ii. The observed background cosmic radiation and the ratio of hydrogen to helium have been shown to be consistent with a universe that was very dense and hot a long time ago and that evolved through different stages as it expanded and cooled (e.g., the formation of nuclei from colliding protons and neutrons predicts the hydrogen-helium ratio [numbers not expected from students], later formation of atoms from nuclei plus electrons, background radiation was a relic from that time).</li> <li>iii. An expanding universe must have been smaller in the past and can be extrapolated back in time to a tiny size from which it expanded.</li> </ul>

## HS-ESS1-4

Students who demonstrate understanding can:

**HS-ESS1-4. Use mathematical or computational representations to predict the motion of orbiting objects in the solar system.** [Clarification Statement: Emphasis is on Newtonian gravitational laws governing orbital motions, which apply to human-made satellites as well as planets and moons.] [Assessment Boundary: Mathematical representations for the gravitational attraction of bodies and Kepler's laws of orbital motions should not deal with more than two bodies, nor involve calculus.]

The performance expectation above was developed using the following elements from *A Framework for K-12 Science Education*:

Science and Engineering Practices	Disciplinary Core Ideas	Crosscutting Concepts
<p><b>Using Mathematical and Computational Thinking</b></p> <p>Mathematical and computational thinking in 9–12 builds on K–8 experiences and progresses to using algebraic thinking and analysis, a range of linear and nonlinear functions including trigonometric functions, exponentials and logarithms, and computational tools for statistical analysis to analyze, represent, and model data. Simple computational simulations are created and used based on mathematical models of basic assumptions.</p> <ul style="list-style-type: none"> <li>Use mathematical or computational representations of phenomena to describe explanations.</li> </ul>	<p><b>ESS1.B: Earth and the Solar System</b></p> <ul style="list-style-type: none"> <li>Kepler's laws describe common features of the motions of orbiting objects, including their elliptical paths around the sun. Orbits may change due to the gravitational effects from, or collisions with, other objects in the solar system.</li> </ul>	<p><b>Scale, Proportion, and Quantity</b></p> <ul style="list-style-type: none"> <li>Algebraic thinking is used to examine scientific data and predict the effect of a change in one variable on another (e.g., linear growth vs. exponential growth).</li> </ul> <p>-----</p> <p style="text-align: center;"><b>Connections to Engineering, Technology, and Applications of Science</b></p> <p><b>Interdependence of Science, Engineering, and Technology</b></p> <ul style="list-style-type: none"> <li>Science and engineering complement each other in the cycle known as research and development (R&amp;D). Many R&amp;D projects may involve scientists, engineers, and others with wide ranges of expertise.</li> </ul>

### Observable features of the student performance by the end of the course:

1	<b>Representation</b>
a	Students identify and describe* the following relevant components in the given mathematical or computational representations of orbital motion: the trajectories of orbiting bodies, including planets, moons, or human-made spacecraft; each of which depicts a revolving body's eccentricity $e = f/d$ , where $f$ is the distance between foci of an ellipse, and $d$ is the ellipse's major axis length (Kepler's first law of planetary motion).
2	<b>Mathematical or computational modeling</b>
a	Students use the given mathematical or computational representations of orbital motion to depict that the square of a revolving body's period of revolution is proportional to the cube of its distance to a gravitational center ( $T^2 \propto R^3$ , where $T$ is the orbital period and $R$ is the semi-major axis of the orbit — Kepler's third law of planetary motion).
3	<b>Analysis</b>
a	Students use the given mathematical or computational representation of Kepler's second law of planetary motion (an orbiting body sweeps out equal areas in equal time) to predict the relationship between the distance between an orbiting body and its star, and the object's orbital velocity (i.e., that the closer an orbiting body is to a star, the larger its orbital velocity will be).

b	Students use the given mathematical or computational representation of Kepler's third law of planetary motion ( $T^2 \propto R^3$ , where T is the orbital period and R is the semi-major axis of the orbit) to predict how either the orbital distance or orbital period changes given a change in the other variable.
c	Students use Newton's law of gravitation plus his third law of motion to predict how the acceleration of a planet towards the sun varies with its distance from the sun, and to argue qualitatively about how this relates to the observed orbits.